



Application Of Differential Equations In Spherical Space

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Abstract

Application of differential equations in spherical space has been approved in this paper.

Regarding the importance of differential equations in mathematical mechanics, a reasonable relation is felt to be presented in order to design and optimize dynamic systems(dynamic mechanics) and all relevant subsets.

This paper tries to establish the relation in question in the simplest possible state.



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Introduction

In dynamic mechanics , the issue of movement relevant to a moving object is discussed and proved , and the dynamic mechanics subset is based on differential equations.

Applications

Regarding the method presented in mathematical , mechanics it can be used to apply differential equations in aerospace science , CNC machine , space ships central control , radars , etc.

Conclusion

In the presented method, it can be concluded that any kind of 1st order differential equations can be applied.

Reference

Elements of Partial Differential Equations, Ian N. Sneddon

The formula

$$\left. \begin{array}{l} \frac{z}{x} = \tan \alpha \\ \frac{z}{y} = \tan \beta \\ \frac{y}{x} = \tan \gamma \end{array} \right\} \tan \alpha = \tan \beta \cdot \tan \gamma$$

$$\frac{dx}{dt} = V_x \quad \frac{dy}{dt} = V_y \quad \frac{dz}{dt} = V_z$$

$\tan \alpha = \tan \beta \cdot \tan \gamma$ is relevant to differential equations images on 3 coordinates OXY, OXZ and OYZ.

N.B.: Extra details have been avoided. The trend of the formulas proof is descriptive enough.



$$1-1 \quad y' + 2y = e^{-x} \Rightarrow Vy/V_x + 2y = e^{-x}, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-2 \quad x^2 y' + 3xy = \frac{\sin x}{x} \Rightarrow x^2 \cdot Vy/V_x + 3xy = \frac{\sin x}{x}, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-3 \quad y' + \frac{y}{x} = 3 \cos^2 x \Rightarrow Vy/V_x + \frac{y}{x} = 3 \cos^2 x, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-4 \quad y' + y = x e^x \Rightarrow Vy/V_x + y = x e^x, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-5 \quad y' + y \tan x = x \sin^2 x \Rightarrow Vy/V_x + y \tan x = x \sin^2 x, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-6 \quad y' + \frac{2xy}{1+x^2} = \frac{1}{1+x^2} \Rightarrow Vy/V_x + \frac{2xy}{1+x^2} = \frac{1}{1+x^2}, V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-7 \quad y' + x^2 y = 1 \Rightarrow Vy/V_x + x^2 y = 1 \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-8 \quad y' + 4y (\tan^2 x) = \tan^2 x \Rightarrow Vy/V_x + 4y (\tan^2 x) = \tan^2 x \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-9 \quad xy' (\log_n x) = x \log_n (x-y) \Rightarrow x \frac{V_x}{V_y} (\log_n x) = x \log_n (x-y) \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-10 \quad y' = (-\cos x)y + 6 \cos^2 x \Rightarrow Vy/V_x = (-\cos x)y + 6 \cos^2 x \Rightarrow$$

$$V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-11 \quad y(zx^2y^3+3)dx + x(x^2y^3-1)dy=0 \Rightarrow y(zx^2y^3+3)\frac{dx}{dt} + x(x^2y^3-1)\frac{dy}{dt} = 0 \Rightarrow y(zx^2y^3+3)V_x + x(x^2y^3-1)V_y =$$

$$0 \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-12 \quad (y^2+yx^2)dx + (x^3-3xy)dy=0 \Rightarrow (y^2+yx^2)\frac{dx}{dt} + (x^3-3xy)\frac{dy}{dt} = 0 \Rightarrow (y^2+yx^2)V_x + (x^3-3xy)V_y = 0 \Rightarrow V =$$

$$\sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-13 \quad Y(2-3xy)dx - xdy=0 \Rightarrow y(2-3xy)\frac{dx}{dt} - x\frac{dy}{dt}=0 \Rightarrow y(2-3xy)V_x - xV_y=0 \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-14 \quad (4xy+3y^4)dx + (2x^2+5xy^3)dy=0 \Rightarrow (4xy+3y^4)\frac{dx}{dt} + (2x^2+5xy^3)\frac{dy}{dt} = 0 \Rightarrow (4xy+3y^4)V_x + (2x^2+5xy^3)V_y=0 \Rightarrow V =$$

$$\sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-15 \quad Y(x^4y-1)dx + x(xy^4-1)dy=0 \Rightarrow y(x^4y-1)\frac{dx}{dt} + x(xy^4-1)\frac{dy}{dt} = 0 \Rightarrow y(x^4y-1)V_x + x(xy^4-1)V_y=0 \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq$$

$$300,000$$

$$1-16 \quad (y^2+2xy+y)dx - (2xy+x^2-x)dy=0 \Rightarrow (y^2+2xy+y)\frac{dx}{dt} - (2xy+x^2-x)\frac{dy}{dt} = 0 \Rightarrow (y^2+2xy+y)V_x - (2xy+x^2-x)V_y =$$

$$0 \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-17 \quad (2x^2y+y^2)dx + (2x^3-xy)dy=0 \Rightarrow (2x^2y+y^2)\frac{dx}{dt} + (2x^3-xy)\frac{dy}{dt}=0 \Rightarrow (2x^2y+y^2)V_x + (2x^3-xy)V_y=0 \Rightarrow$$

$$V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$



$$1-18 \quad y(4x+3y^2)dx+x(2x+4y^2)dy=0 \Rightarrow y(4x+3y^2)\frac{dx}{dt}+x(2x+4y^2)\frac{dy}{dt}=0 \Rightarrow y(4x+3y^2)Vx+x(2x+4y^2)Vy=0 \Rightarrow V=\sqrt{V_x^2+V_y^2}, 0$$

$$<V \leq 300,000$$

$$1-19 \quad \frac{dy}{dx} = \frac{-y(\tan x + \log_n y)}{\tan x} \Rightarrow \frac{dy/dt}{dx/dt} = \frac{-y(\tan x + \log_n y)}{\tan x} \Rightarrow \frac{Vy}{Vx} = \frac{-y(\tan x + \log_n y)}{\tan x} \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$

$$1-20 \quad \frac{dy}{dx} = \frac{(zy+3xy^2)}{3x+4yx^2} \Rightarrow \frac{dy/dt}{dx/dt} = -\frac{zy+3xy^2}{3x+4yx^2} \Rightarrow \frac{Vy}{Vx} = \frac{2y+3xy^2}{3x+4yx^2} \Rightarrow V = \sqrt{V_x^2 + V_y^2}, 0 < V \leq 300,000$$





$$\mathbf{2-1} \quad Y \cdot dx + X \cdot dy + 2 \cdot Z \cdot dz = 0 \Rightarrow$$

$$Y \cdot \frac{dx}{dt} + X \cdot \frac{dy}{dt} + 2 \cdot Z \cdot \frac{dz}{dt} = 0$$

$$Y \cdot V_x + X \cdot V_y + 2 \cdot Z \cdot V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-2} \quad Z \cdot (z + y) dx + z \cdot (z + x) dy - 2 \cdot X \cdot dz = 0$$

$$Z \cdot (z + y) \frac{dx}{dt} + Z \cdot (z + x) \frac{dy}{dt} - 2 \cdot X \cdot \frac{dz}{dt} = 0$$

$$Z(z + y) \cdot V_x + Z(z + x) \cdot V_y - 2 \cdot X \cdot V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-3} \quad Y \cdot Z \cdot dx + 2 \cdot X \cdot Z \cdot dy - 3 \cdot X \cdot Y \cdot dz = 0$$

$$Y \cdot Z \cdot \frac{dx}{dt} + 2 \cdot X \cdot Z \cdot \frac{dy}{dt} - 3 \cdot X \cdot Y \cdot \frac{dz}{dt} = 0$$

$$Y \cdot Z \cdot V_x + 2 \cdot X \cdot Z \cdot V_y - 3 \cdot X \cdot Y \cdot V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-4} \quad 2 \cdot X \cdot Z \cdot dx + Z \cdot dy - dz = 0$$

$$2 \cdot X \cdot Z \frac{dx}{dt} + Z \cdot \frac{dy}{dt} - \frac{dz}{dt} = 0$$

$$2 \cdot X \cdot Z \cdot V_x + Z \cdot V_y - V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-5} \quad (Y^2 + X \cdot Z) \cdot dx + (X^2 + Y \cdot Z) \cdot dy + 3 \cdot Z^2 \cdot dz = 0$$

$$(Y^2 + X \cdot Z) \cdot \frac{dx}{dt} + (X^2 + Y \cdot Z) \cdot \frac{dy}{dt} + 3 \cdot Z^2 \cdot \frac{dz}{dt} = 0$$

$$(Y^2 + X \cdot Z) \cdot V_x + (X^2 + Y \cdot Z) \cdot V_y + 3 \cdot Z^2 \cdot V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



2-6 $(X^2.Z-Y^3).dx + 3.X.Y^2.dy + X^3.dz = 0$

$$(X^2.Z-Y^3). \frac{dx}{dt} + 3.X.Y^2. \frac{dy}{dt} + X^3. \frac{dz}{dt} = 0$$

$$(X^2.Z-Y^3).V_x + 3.X.Y^2.V_y + X^3.V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-7 $a^2.y^2.z^2.d x + b^2.z^2.x^2.d y + c^2.x^2.y^2.d z = 0$

$$a^2.y^2.z^2. \frac{dx}{dt} + b^2.z^2.x^2. \frac{dy}{dt} + c^2.x^2.y^2. \frac{dz}{dt} = 0$$

$$a^2.y^2.z^2.V_x + b^2.z^2.x^2.V_y + c^2.x^2.y^2.V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-8 $X(y^2-a^2).dx + Y(x^2-z^2).dy - z(y^2-a^2).dz = 0$

$$X(y^2-a^2). \frac{dx}{dt} + Y(x^2-z^2). \frac{dy}{dt} - z(y^2-a^2). \frac{dz}{dt} = 0$$

$$X(y^2-a^2).V_x + Y(x^2-z^2).V_y - z(y^2-a^2).V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-9 $Y.Z(y+z).dx + X.Z.(x+z).dy + X.Y(x+y).dz = 0$

$$Y.Z(y+z). \frac{dx}{dt} + X.Z.(x+z). \frac{dy}{dt} + X.Y(x+y). \frac{dz}{dt} = 0$$

$$Y.Z(y+z).V_x + X.Z.(x+z).V_y + X.Y(x+y).V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-10 $Z(z+y^2).dx + Z(z+x^2).dy - X.Y.(x+y).dz = 0$

$$Z(z+y^2). \frac{dx}{dt} + Z(z+x^2). \frac{dy}{dt} - X.Y.(x+y). \frac{dz}{dt} = 0$$

$$Z(z+y^2).V_x + Z(z+x^2).V_y - X.Y.(x+y).V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



2-11 $(y+z).dx + (z+x).dy + (x+y).dz = 0$

$$(y+z). \frac{dx}{dt} + (z+x). \frac{dy}{dt} + (x+y). \frac{dz}{dt} = 0$$

$$(y+z).V_x + (z+x).V_y + (x+y).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-12 $Z.Y(a-x).dx + [z-y^2 + (a-x)^2].dy - Y.dz = 0$

$$Z.Y(a-x). \frac{dx}{dt} + [z-y^2 + (a-x)^2]. \frac{dy}{dt} - Y. \frac{dz}{dt} = 0$$

$$Z.Y(a-x).V_x + [z-y^2 + (a-x)^2].V_y - Y.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-13 $Y.(1+z^2).dx + X.(1+z^2).dy + (x^2+y^2).dz = 0$

$$Y.(1+z^2). \frac{dx}{dt} + X.(1+z^2). \frac{dy}{dt} + (x^2+y^2). \frac{dz}{dt} = 0$$

$$Y.(1+z^2).V_x + X.(1+z^2).V_y + (x^2+y^2).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-14 $(y^2 + y.z + z^2).dx + (z^2 + z.x + x^2).dy + (x^2 + x.y + y^2).dz = 0$

$$(y^2 + y.z + z^2). \frac{dx}{dt} + (z^2 + z.x + x^2). \frac{dy}{dt} + (x^2 + x.y + y^2). \frac{dz}{dt} = 0$$

$$(y^2 + y.z + z^2).V_x + (z^2 + z.x + x^2).V_y + (x^2 + x.y + y^2).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-15 $Y.Z.dx + X.Z.dy + X.Y.dz = 0$

$$Y.Z. \frac{dx}{dt} + X.Z. \frac{dy}{dt} + X.Y. \frac{dz}{dt} = 0$$

$$Y.Z.V_x + X.Z.V_y + X.Y.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



$$2-16 \quad (1+y+z).dx + X.(z-x).dy - (1+x.y).dz = 0$$

$$(1+y+z). \frac{dx}{dt} + X.(z-x). \frac{dy}{dt} - (1+x.y). \frac{dz}{dt} = 0$$

$$(1+y+z).V_x + X.(z-x).V_y - (1+x.y).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-17 \quad Y.(x+4).(y+z).dx - X.(y+3.z).dy + 2.X.Y.dz = 0$$

$$Y.(x+4).(y+z). \frac{dx}{dt} - X.(y+3.z). \frac{dy}{dt} + 2.X.Y. \frac{dz}{dt} = 0$$

$$Y.(x+4).(y+z).V_x - X.(y+3.z).V_y + 2.X.Y.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-18 \quad Y.Z.dx + (x^2-y-z.x).dy + (x^2.z-x.y).dz = 0$$

$$Y.Z. \frac{dx}{dt} + (x^2-y-z.x). \frac{dy}{dt} + (x^2.z-x.y). \frac{dz}{dt} = 0$$

$$Y.Z.V_x + (x^2-y-z.x).V_y + (x^2.z-x.y).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-19 \quad 2.Y.Z.dx - 2.X.Z.dy - (X^2-Y^2).(Z-1).dz = 0$$

$$2.Y.Z. \frac{dx}{dt} - 2.X.Z. \frac{dy}{dt} - (X^2-Y^2).(Z-1). \frac{dz}{dt} = 0$$

$$2.Y.Z.V_x - 2.X.Z.V_y - (X^2-Y^2).(Z-1).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-20 \quad \frac{dx}{y^3x-2.x^4} = \frac{dy}{2.y^4-x^3.y} = \frac{dz}{2.z.(x^3-y^3)}$$

$$\frac{dx/dt}{y^3.x-2.x^4} = \frac{dy/dt}{2.y^4-x^3.y} = \frac{dz/dt}{2.z.(x^3-y^3)}$$

$$\frac{V_x}{y^3.x-2.x^4} = \frac{V_y}{2.y^4-x^3.y} = \frac{V_z}{2.z.(x^3-y^3)}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



$$2-21 \quad \frac{dx}{2.x.z} = \frac{dy}{2.y.z} = \frac{dz}{z^2 - x^2 - y^2}$$

$$\frac{dx/dt}{2.x.z} = \frac{dy/dt}{2.y.z} = \frac{dz/dt}{z^2 - x^2 - y^2}$$

$$\frac{Vx}{2.x.z} = \frac{Vy}{2.y.z} = \frac{Vz}{z^2 - x^2 - y^2}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-22 \quad \frac{dx}{x+y} = \frac{dy}{x+y} = \frac{dz}{-(x+y+2.z)}$$

$$\frac{dx/dt}{x+y} = \frac{dy/dt}{x+y} = \frac{dz/dt}{-(x+y+2.z)}$$

$$\frac{Vx}{x+y} = \frac{Vy}{x+y} = \frac{Vz}{-(x+y+2.z)}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-23 \quad \frac{dx}{c.y-b.z} = \frac{dy}{a.z-c.x} = \frac{dz}{b.x-z.y}$$

$$\frac{dx/dt}{c.y-b.z} = \frac{dy/dt}{a.z-c.x} = \frac{dz/dt}{b.x-z.y}$$

$$\frac{Vx}{c.y-b.z} = \frac{Vy}{a.z-c.x} = \frac{Vz}{b.x-z.y}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-24 \quad \frac{dx}{x^2+a^2} = \frac{dy}{x.y-a.z} = \frac{dz}{x.z+a.y}$$

$$\frac{dx/dt}{x^2+a^2} = \frac{dy/dt}{x.y-a.z} = \frac{dz/dt}{x.z+a.y}$$

$$\frac{Vx}{x^2+a^2} = \frac{Vy}{x.y-a.z} = \frac{Vz}{x.z+a.y}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

a = cte



2-25 $z.y.dx - z.x.dy - y^2.dz = 0$

$$z.y.\frac{dx}{dt} - z.x.\frac{dy}{dt} - y^2.\frac{dz}{dt} = 0$$

$$z.y.V_x - z.x.V_y - y^2.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-26 $(y^2 + z^2).dx + x.y.dy + x.z.dz = 0$

$$(y^2 + z^2).\frac{dx}{dt} + x.y.\frac{dy}{dt} + x.z.\frac{dz}{dt} = 0$$

$$(y^2 + z^2).V_x + x.y.V_y + x.z.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-27 $(Y + Z).dx + dy + dz = 0$

$$(Y + Z).\frac{dx}{dt} + \frac{dy}{dt} + \frac{dz}{dt} = 0$$

$$(Y + Z).V_x + V_y + V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-28 $(2.x.y.z + z^2).dx + x^2.z.dy + (x.z + 1).dz = 0$

$$(2.x.y.z + z^2).\frac{dx}{dt} + x^2.z.\frac{dy}{dt} + (x.z + 1).\frac{dz}{dt} = 0$$

$$(2.x.y.z + z^2).V_x + x^2.z.V_y + (x.z + 1).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-29 $z.y^2.dx + z.x^2.dy - x^2y^2.dz = 0$

$$z.y^2.\frac{dx}{dt} + z.x^2.\frac{dy}{dt} - x^2y^2.\frac{dz}{dt} = 0$$

$$z.y^2.V_x + z.x^2.V_y - x^2y^2.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



$$\mathbf{2-30} \quad X.(y^2 - z^2).dx + y^2(z^2 - x^2).dy + z.(x^2 - y^2).dz = 0$$

$$X.(y^2 - z^2). \frac{dx}{dt} + y^2(z^2 - x^2). \frac{dy}{dt} + z.(x^2 - y^2). \frac{dz}{dt} = 0$$

$$X.(y^2 - z^2).V_x + y^2(z^2 - x^2).V_y + z.(x^2 - y^2).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-31} \quad (y^2 - z^2).dx + (x^2 - z^2).dy + (x + y).(x + y + 2.z).dz = 0$$

$$(y^2 - z^2). \frac{dx}{dt} + (x^2 - z^2). \frac{dy}{dt} + (x + y).(x + y + 2.z). \frac{dz}{dt} = 0$$

$$(y^2 - z^2).V_x + (x^2 - z^2).V_y + (x + y).(x + y + 2.z).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-32} \quad (y^2 + y.z).dx + (x.z + z^2).dy + (y^2 - x.y).dz = 0$$

$$(y^2 + y.z). \frac{dx}{dt} + (x.z + z^2). \frac{dy}{dt} + (y^2 - x.y). \frac{dz}{dt} = 0$$

$$(y^2 + y.z).V_x + (x.z + z^2).V_y + (y^2 - x.y).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-33} \quad 2.z.(y + z).dx - 2.x.z.dy - [(y + z)^2 - x^2 - 2.x.z].dz = 0$$

$$2.z.(y + z). \frac{dx}{dt} - 2.x.z. \frac{dy}{dt} - [(y + z)^2 - x^2 - 2.x.z]. \frac{dz}{dt} = 0$$

$$2.z.(y + z).V_x - 2.x.z.V_y - [(y + z)^2 - x^2 - 2.x.z].V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-34} \quad (x^2 + x.y + y.z).dx - x.(x + z).dy + x^2.dz = 0$$

$$(x^2 + x.y + y.z). \frac{dx}{dt} - x.(x + z). \frac{dy}{dt} + x^2. \frac{dz}{dt} = 0$$

$$(x^2 + x.y + y.z).V_x - x.(x + z).V_y + x^2.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$





2-35 $y.z(1+4.x.z).dx+x.z.(1+2.x.z).dy+x.y.dz=0$

$$y.z(1+4.x.z).\frac{dx}{dt} + x.z.(1+2.x.z).\frac{dy}{dt} + x.y.\frac{dz}{dt} = 0$$

$$y.z(1+4.x.z).V_x+x.z.(1+2.x.z).V_y + x.y.V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-36 $(2.x.z+z^2).dx + 2.y.z.dy - (2.x^2 + 2.y^2+x.z - z.a^2).dz = 0$

$$(2.x.z+z^2).\frac{dx}{dt} + 2.y.z.\frac{dy}{dt} + (2.x^2 + 2.y^2+x.z - z.a^2).\frac{dz}{dt} = 0$$

$$(2.x.z+z^2).V_x + 2.y.z.V_y + (2.x^2 + 2.y^2+x.z - z.a^2).V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-37 $(y.dx + x.dy).(a - z)+x.y. dz = 0$

$$(y.\frac{dx}{dt} + x.\frac{dy}{dt}).(a - z) + x.y.\frac{dz}{dt} = 0$$

$$(y.V_x + x.V_y).(a - z) + x.y.V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

 $a = \text{cte}$

2-38 $2.x.dx+(2.x^2.z+2.y.z+2.y^2+1).dy+dz=0$

$$2.x.\frac{dx}{dt} + (2.x^2.z+2.y.z+2.y^2+1).\frac{dy}{dt} + \frac{dz}{dt} = 0$$

$$2.x.V_x + (2.x^2.z+2.y.z+2.y^2+1).V_y + V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

2-39 $2.x.z.(y - z). dx - z.(x^2+2.z).dy + y.(x^2 + z.y). dz = 0$

$$2.x.z.(y - z).\frac{dx}{dt} - z.(x^2+2.z).\frac{dy}{dt} + y.(x^2 + z.y).\frac{dz}{dt} = 0$$

$$2.x.z.(y - z).V_x - z.(x^2+2.z).V_y + y.(x^2 + z.y).V_z = 0$$

$$V_T = \sqrt{V^2_x + V^2_y + V^2_z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$



$$\mathbf{2-40} \quad (12.x + 29.y).z.dx - (11.x + 12.y).z.dy - (2.x^2 + 3.x.y - z.y^2).dz = 0$$

$$(12.x + 29.y).z. \frac{dx}{dt} - (11.x + 12.y).z. \frac{dy}{dt} - (2.x^2 + 3.x.y - z.y^2). \frac{dz}{dt} = 0$$

$$(12.x + 29.y).z.Vx - (11.x + 12.y).z. Vy - (2.x^2 + 3.x.y - z.y^2). Vz = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-41} \quad y.dx - x.dy + dz = 0$$

$$y. \frac{dx}{dt} - x. \frac{dy}{dt} + \frac{dz}{dt} = 0$$

$$y.Vx - x.Vy + Vz = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-42} \quad \frac{dx}{y-z} = \frac{dy}{z-x} = \frac{dz}{x-y}$$

$$\frac{dx/dt}{y-z} = \frac{dy/dt}{z-x} = \frac{dz/dt}{x-y}$$

$$\frac{Vx}{y-z} = \frac{Vy}{z-x} = \frac{Vz}{x-y}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-43} \quad dx + dy + dz = 0$$

$$\frac{dx}{dt} + \frac{dy}{dt} + \frac{dz}{dt} = 0$$

$$Vx + Vy + Vz = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-44} \quad x.dx + y.dy + z.dz = 0$$

$$x. \frac{dx}{dt} + y. \frac{dy}{dt} + z. \frac{dz}{dt} = 0$$

$$x.Vx + y. Vy + z. Vz = 0$$



$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-45 \frac{dx}{x.(y^2+z)} = \frac{dy}{-y.(x^2+z)} = \frac{dz}{(x^2-y^2).z}$$

$$\frac{dx/dt}{x.(y^2+z)} = \frac{dx/dt}{-y.(x^2+z)} = \frac{dx/dt}{(x^2-y^2).z}$$

$$\frac{Vx}{x.(y^2+z)} = \frac{Vy}{-y.(x^2+z)} = \frac{Vz}{(x^2-y^2).z}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-46 \frac{dx}{dt} = Vx = 2.z - 4.x \quad V_T=?$$

$$\frac{dy}{dt} = Vy = 2.z - 2.y$$

$$\frac{dz}{dt} = Vz = 2.x + 2.y - 3.z$$

$$V_T = \sqrt{V^2x + V^2y + V^2z} = \sqrt{(2.z - 4.x)^2 + (2.z - 2.y)^2 + (2.x + 2.y - 3.z)^2}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-47 \frac{dx}{dt} = (z - 2.y) \quad V_T=?$$

$$\frac{dy}{dt} = (z - x)$$

$$\frac{dz}{dt} = (x + y - 2.z)$$

$$V_T = \sqrt{(z - 2.y)^2 + (z - x)^2 + (x + y - 2.z)^2}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-48 \frac{dx}{dt} = (2.y - z)$$

$$\frac{dy}{dt} = (y - x)$$

$$\frac{dz}{dt} = (y + z - x)$$

$$V_T = \sqrt{(2.y - z)^2 + (y - x)^2 + (y + z - x)^2}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$



$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\left. \begin{aligned} 2-49 \quad \frac{dx}{dt} &= (z - 2.x) \\ \frac{dy}{dt} &= (z - x) \\ \frac{dz}{dt} &= (3.x + 3.y + 3.z) \end{aligned} \right\}$$

$$V_T = \sqrt{(z - 2.x)^2 + (z - x)^2 + (3.x + 3.y + 3.z)^2}$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-50 \quad (x + a)^2 + (y - b)^2 + z^2 = 1$$

$$2.(x + a).dx + 2.(y - b).dy + 2.z.dz = 0$$

$$2.(x+a). \frac{dx}{dt} + 2.(y-b). \frac{dy}{dt} + 2.z. \frac{dz}{dt} = 0$$

$$2.(x + a).V_x + 2.(y - b).V_y + 2.z.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$2-51 \quad Z = (x + a).(y + b) = x.y + b.x + a.y + a.b$$

$$dz = x.dy + y.dx + b.dx + a.dy + 0 = (x + a).dy + y.dx + b.dx$$

$$\frac{dz}{dt} = (x + a). \frac{dy}{dt} + (y + b). \frac{dx}{dt}$$

$$V_z = (x + a).V_y + (y + b).V_x$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$V_T = ?$$

$$a = \text{cte}$$

$$b = \text{cte}$$

$$2-52 \quad 2.z = (ax + y)^2 + b$$

$$V_T = ?$$

$$a = \text{cte}$$

$$2.z = (a^2.x^2 + y^2 + 2.a.x.y) + b$$

$$b = \text{cte}$$

$$2.dz = 2.a^2.x.dx + 2.y.dy + 2.a.x.dy + 2.a.y.dx$$

$$2.dz = (2.a^2.x + 2.a.y).dx + (2.y + 2.a.x).dy$$

$$2. \frac{dz}{dt} = (2.a^2.x + 2.a.y). \frac{dx}{dt} + (2.y + 2.a.x). \frac{dy}{dt}$$

$$2.V_z = (2.a^2.x + 2.a.y).V_x + (2.y + 2.a.x).V_y$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$



$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$\mathbf{2-53} \quad a.x^2 + b.y^2 + z^2 = 1$$

$$2.a.x.dx + 2.b.y.dy + 2.z.dz = 0$$

$$2.a.x.\frac{dx}{dt} + 2.b.y.\frac{dy}{dt} + 2.z.\frac{dz}{dt} = 0$$

$$2.a.x.V_x + 2.b.y.V_y + 2.z.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$V_T = ?$$

$$a = \text{cte}$$

$$b = \text{cte}$$

$$\mathbf{2-54} \quad x^2 + y^2 + z^2 = C$$

$$2.x.dx + 2.y.dy + 2.z.dz = 0$$

$$2.x.\frac{dx}{dt} + 2.y.\frac{dy}{dt} + 2.z.\frac{dz}{dt} = 0$$

$$2.x.V_x + 2.y.V_y + 2.z.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$V_T = ?$$

$$c = \text{cte}$$

$$\mathbf{2-55} \quad x.(y^2 + z) - y.(x^2 + z) = (x^2 - y^2)z$$

$$x.y^2 + x.z - y.x^2 - y.z = x^2.z - y^2.z$$

$$2.x.y.dy + y^2.dx + x.dz + z.dx - 2.y.x.dx - x^2.dy - y.dz - z.dy = 2.x.z.dx + x^2.dz - 2.y.z.dy - y^2.dz$$

$$(2.x.y - x^2 - z + 2.y.z).dy + (y^2 + z - 2.y.x - 2.x.z).dx + (x - y - x^2 + y^2).dz = 0$$

$$(2.x.y - x^2 - z + 2.y.z).\frac{dy}{dt} + (y^2 + z - 2.y.x - 2.x.z).\frac{dx}{dt} + (x - y - x^2 + y^2).\frac{dz}{dt} = 0$$

$$(2.x.y - x^2 - z + 2.y.z).V_y + (y^2 + z - 2.y.x - 2.x.z).V_x + (x - y - x^2 + y^2).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$V_T = ?$$

$$\mathbf{2-56} \quad x^2 + y^2 - 2.z = C$$

$$2.x.dx + 2.y.dy - 2.dz = 0$$

$$2.x.\frac{dx}{dt} + 2.y.\frac{dy}{dt} - 2.\frac{dz}{dt} = 0$$

$$2.x.V_x + 2.y.V_y - 2.V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec}$$

$$V_T = ?$$

$$c = \text{cte}$$



$$2-57 \quad x^2 + y^2 + 2.x.y.z - 2.z + 2 = 0$$

$$2.x.dx + 2.y.dy + 2.y.z.dx + 2.x.y.dz + 2.x.z.dy - 2.dz = 0$$

$$(2.x + 2.y.z).dx + (2.y + 2.x.z).dy + (2.x.y - 2).dz = 0$$

$$(2.x + 2.y.z). \frac{dx}{dt} + (2.y + 2.x.z). \frac{dy}{dt} + (2.x.y - 2). \frac{dz}{dt} = 0$$

$$(2.x + 2.y.z).V_x + (2.y + 2.x.z).V_y + (2.x.y - 2).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec} \quad V_T = ?$$

$$2-58 \quad 2.y.(z - 3) + (2.x - z) = y.(2.x - 3)$$

$$2.y.z - 6.y + 2.x - z = 2.y.x - 3y$$

$$2.y.dz + 2.z.dy - 6.dy + 2.dx - dz = 2.y.dx + 2.x.dy - 3dy$$

$$(2.y - 1).dz + (2.z - 6 - 2.x + 3).dy + (2 - 2.y).dx = 0$$

$$(2.y - 1). \frac{dz}{dt} + (2.z - 6 - 2.x + 3). \frac{dy}{dt} + (2 - 2.y). \frac{dx}{dt} = 0$$

$$(2.y - 1).V_z + (2.z - 6 - 2.x + 3).V_y + (2 - 2.y).V_x = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec} \quad V_T = ?$$

$$2-59 \quad (2.x.y - 1) + (z - 2.x^2) = 2(x - yz)$$

$$2.x.dy + 2.y.dx + dz - 4.x.dx = 2.dx - 2.y.dz - 2.z.dy$$

$$(2.x + 2.z).dy + (2.y - 4.x - 2).dx + (1 + 2.y).dz = 0$$

$$(2.x + 2.z). \frac{dy}{dt} + (2.y - 4.x - 2). \frac{dx}{dt} + (1 + 2.y). \frac{dz}{dt} = 0$$

$$(2.x + 2.z).V_y + (2.y - 4.x - 2).V_x + (1 + 2.y).V_z = 0$$

$$V_T = \sqrt{V^2x + V^2y + V^2z}$$

$$0 < V_T \leq 300,000 \text{ Km/Sec} \quad V_T = ?$$